

### The Solubility Product Constant ( $K_{sp}$ )

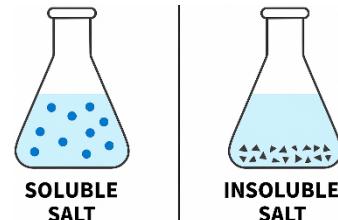
Read from Lesson 1: Solubility of Salts in the Chemistry Tutorial Section, Chapter 16 of The Physics

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Part b: [Solubility and  \$K\_{sp}\$](#)

#### Soluble vs. Insoluble Salts

- Salts are ionic compounds formed from cations and anions.
- **Soluble salts** dissolve readily in water; they dissociate completely.
- **Insoluble salts** dissolve only slightly: they reach a **saturation point** where no more ions can dissolve.
- Even “insoluble” salts dissolve a little—these are called **sparingly soluble** or **slightly soluble**.
- Use **solubility rules** to predict whether a salt will dissolve.



#### Dissociation of Salts

- Dissociation: the process of a salt breaking into ions when it dissolves.
- $\text{Na}_3\text{PO}_4(s) \rightarrow 3 \text{Na}^+(aq) + \text{PO}_4^{3-}(aq)$  (*This is a soluble salt: 100% dissociated*)
- $\text{PbCl}_2(s) \rightleftharpoons \text{Pb}^{2+}(aq) + 2 \text{Cl}^-(aq)$  (*This is an insoluble salt: not 100% dissociated*)
  - Adding excess  $\text{PbCl}_2$  to water results in a saturated solution with undissolved solid remaining.

#### The Solubility Product Constant ( $K_{sp}$ )

- $K_{sp}$  quantifies the extent to which an insoluble salt dissolves.
- Larger  $K_{sp}$  → greater solubility.
- $K_{sp}$  for lead (II) chloride:  $\text{PbCl}_2(s) \rightleftharpoons \text{Pb}^{2+}(aq) + 2 \text{Cl}^-(aq)$  is  $K_{sp} = [\text{Pb}^{2+}] * [\text{Cl}^-]^2$  (\*\*remember, solids are omitted from equilibrium expressions)

#### Calculating Ion Concentrations from $K_{sp}$

1. Write the balanced dissociation equation.
2. Write the  $K_{sp}$  expression.
3. Set up an ICE table (Initial, Change, Equilibrium).
4. Substitute values and solve for x (amount dissolved).
5. Use algebra to find ion concentrations.

**Example:** The  $K_{sp}$  for  $\text{PbCl}_2$  is  $1.7 \times 10^{-5}$  at  $25^\circ\text{C}$ . Determine the ion concentrations at equilibrium.

	$\text{PbCl}_2(s)$	$\rightleftharpoons$	$\text{Pb}^{2+}(aq)$	+	$2 \text{Cl}^-(aq)$
<b>Initial</b>	Does not matter		0		0
<b>Change</b>	$-x$		$+x$		$+2x$
<b>Equilibrium</b>	Does not matter		$x$		$2x$

$$K_{sp} = 1.7 \times 10^{-5} = [\text{Pb}^{2+}] * [\text{Cl}^-]^2 = (x) * (2x)^2$$

$$x = 0.016, \text{ so } [\text{Pb}^{2+}] = 0.016 \text{ M,}$$

$$K_{sp} = 1.7 \times 10^{-5} = 4x^3$$

$$2x = 0.032 \text{ so } [\text{Cl}^-] = 0.032 \text{ M}$$

#### Molar Solubility

- **Definition:** Moles of salt that dissolve per liter of water. (Can be found by solving for x in the ICE table.)
- Reverse Calculations: find  $K_{sp}$  from molar solubility by using the same steps as above, but in reverse.

#### Solubility (g/L)

- Convert molar solubility to grams/L using molar mass.

## Solution Equilibria

### Questions

1. Use the solubility rules to determine whether each of the following salts is **soluble** or **insoluble** in water. For each compound: write its correct **chemical formula** and then label it as **soluble** or **insoluble**.

Compound Name	Chemical Formula	Solubility (Soluble / Insoluble)
a. Magnesium bromide		
b. Iron(II) carbonate		
c. Chromium(III) hydroxide		
d. Ammonium sulfate		
e. Silver iodide		
f. Tin(IV) sulfite		
g. Barium acetate		
h. Copper(II) sulfide		
i. Calcium phosphate		
j. Potassium hydroxide		

2. From your list in Question 1, choose the compounds you identified as **insoluble** in water. For each one, complete the table below:

Compound Formula	Dissociation Equation	$K_{sp}$ Expression
Example: $\text{BaSO}_4$	$\text{BaSO}_4(s) \rightleftharpoons \text{Ba}^{2+}(aq) + \text{SO}_4^{2-}(aq)$	$K_{sp} = [\text{Ba}^{2+}][\text{SO}_4^{2-}]$

## Solution Equilibria

3. Sophie Soluble and Aaron Agin are debating the solubility of lead(II) compounds. Sophie claims lead(II) carbonate is less soluble than lead(II) chloride due to its smaller  $K_{sp}$ . Aaron disagrees, arguing that lead(II) carbonate is more soluble because it dissociates into fewer ions. How can Sophie clarify that  $K_{sp}$  —not ion count—determines solubility?



4. Use tools such as a dissociation equation, an ICE table, a  $K_{sp}$  expression, and good algebra skills to calculate ion concentrations in the following solutions.

- 0.50 M potassium carbonate
- 0.33 M aluminum bromide
- a saturated solution of silver acetate at 25°C. ( $K_{sp} = 1.9 \times 10^{-3}$ )
- a saturated solution of calcium hydroxide at 25°C. ( $K_{sp} = 5.0 \times 10^{-6}$ )
- a saturated solution of magnesium phosphate at 25°C. ( $K_{sp} = 1.0 \times 10^{-24}$ )

## Solution Equilibria

5. Use tools such as a dissociation equation, an ICE table, a  $K_{sp}$  expression, and good algebra skills to calculate the  $K_{sp}$  for the following compounds:

- A saturated solution of calcium fluoride has the following ion concentrations at equilibrium:  
 $[Ca^{2+}] = 2.1 \times 10^{-4} M$  and  $[F^-] = 4.2 \times 10^{-4} M$
- In a saturated solution of lead(II) hydroxide, the  $[OH^-]$  is measured to be  $3.0 \times 10^{-7} M$ .
- The molar solubility of magnesium hydroxide is  $1.12 \times 10^{-4} mol/L$  at  $25^\circ C$ .

6. Calculate the solubility of the following solutions.

- Copper(I) chloride in mol/L ( $K_{sp} = 1.7 \times 10^{-7}$ )
- Magnesium fluoride in g/L ( $K_{sp} = 5.2 \times 10^{-11}$ )
- Calcium iodate in g/L ( $K_{sp} = 6.5 \times 10^{-6}$ )