

## The Solubility Product Constant ( $K_{sp}$ )

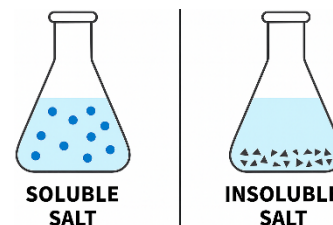
Read from **Lesson 1: Solubility of Salts** in the **Chemistry Tutorial** Section, **Chapter 16** of **The Physics**

Classroom: Part a: [The Solubility Product Constant,  \$K\_{sp}\$](#)

Part b: [Solubility and  \$K\_{sp}\$](#)

### Soluble vs. Insoluble Salts

- **Salts** are ionic compounds formed from cations and anions.
- **Soluble salts** dissolve readily in water; they dissociate completely.
- **Insoluble salts** dissolve only slightly: they reach a **saturation point** where no more ions can dissolve.
- Even “insoluble” salts dissolve a little—these are called **sparingly soluble** or **slightly soluble**.
- Use **solubility rules** to predict whether a salt will dissolve.



### Dissociation of Salts

- Dissociation: the process of a salt breaking into ions when it dissolves.
- $\text{Na}_3\text{PO}_4(s) \rightarrow 3 \text{Na}^+(aq) + \text{PO}_4^{3-}(aq)$  (This is a **soluble** salt: 100% dissociated)
- $\text{PbCl}_2(s) \rightleftharpoons \text{Pb}^{2+}(aq) + 2 \text{Cl}^-(aq)$  (This is an **insoluble** salt: not 100% dissociated)
  - Adding excess  $\text{PbCl}_2$  to water results in a saturated solution with undissolved solid remaining.

### The Solubility Product Constant ( $K_{sp}$ )

- $K_{sp}$  quantifies the extent to which an insoluble salt dissolves.
- Larger  $K_{sp} \rightarrow$  greater solubility.
- $K_{sp}$  for lead (II) chloride:  $\text{PbCl}_2(s) \rightleftharpoons \text{Pb}^{2+}(aq) + 2 \text{Cl}^-(aq)$  is  $K_{sp} = [\text{Pb}^{2+}] * [\text{Cl}^-]^2$  (\*\*remember, solids are omitted from equilibrium expressions)

### Calculating Ion Concentrations from $K_{sp}$

1. Write the balanced dissociation equation.
2. Write the  $K_{sp}$  expression.
3. Set up an ICE table (Initial, Change, Equilibrium).
4. Substitute values and solve for  $x$  (amount dissolved).
5. Use algebra to find ion concentrations.

**Example:** The  $K_{sp}$  for  $\text{PbCl}_2$  is  $1.7 \times 10^{-5}$  at  $25^\circ\text{C}$ . Determine the ion concentrations at equilibrium.

|                    | $\text{PbCl}_2(s)$ | $\rightleftharpoons$ | $\text{Pb}^{2+}(aq)$ | + | $2 \text{Cl}^-(aq)$ |
|--------------------|--------------------|----------------------|----------------------|---|---------------------|
| <b>Initial</b>     | Does not matter    |                      | 0                    |   | 0                   |
| <b>Change</b>      | -x                 |                      | + x                  |   | + 2x                |
| <b>Equilibrium</b> | Does not matter    |                      | x                    |   | 2x                  |

$$K_{sp} = 1.7 \times 10^{-5} = [\text{Pb}^{2+}] * [\text{Cl}^-]^2 = (x) * (2x)^2$$

$$x = 0.016, \text{ so } [\text{Pb}^{2+}] = \mathbf{0.016 \text{ M}},$$

$$K_{sp} = 1.7 \times 10^{-5} = 4x^3$$

$$2x = 0.032 \text{ so } [\text{Cl}^-] = \mathbf{0.032 \text{ M}}$$

### Molar Solubility

- **Definition:** Moles of salt that dissolve per liter of water. (Can be found by solving for  $x$  in the ICE table.)
- Reverse Calculations: find  $K_{sp}$  from molar solubility by using the same steps as above, but in reverse.

### Solubility (g/L)

- Convert molar solubility to grams/L using molar mass.

## Solution Equilibria

### Questions

1. Use the solubility rules to determine whether each of the following salts is **soluble** or **insoluble** in water. For each compound: write its correct **chemical formula** and then label it as **soluble** or **insoluble**.

| Compound Name              | Chemical Formula | Solubility (Soluble / Insoluble) |
|----------------------------|------------------|----------------------------------|
| a. Magnesium bromide       |                  |                                  |
| b. Iron(II) carbonate      |                  |                                  |
| c. Chromium(III) hydroxide |                  |                                  |
| d. Ammonium sulfate        |                  |                                  |
| e. Silver iodide           |                  |                                  |
| f. Tin(IV) sulfite         |                  |                                  |
| g. Barium acetate          |                  |                                  |
| h. Copper(II) sulfide      |                  |                                  |
| i. Calcium phosphate       |                  |                                  |
| j. Potassium hydroxide     |                  |                                  |

2. From your list in Question 1, choose the compounds you identified as **insoluble** in water. For each one, complete the table below:

| Compound Formula  | Dissociation Equation                                      | $K_{sp}$ Expression             |
|-------------------|--|---------------------------------|
| Example: $BaSO_4$ | $BaSO_4(s) \rightleftharpoons Ba^{2+}(aq) + SO_4^{2-}(aq)$ | $K_{sp} = [Ba^{2+}][SO_4^{2-}]$ |
|                   |  |                                 |
|                   |  |                                 |
|                   |  |                                 |
|                   |  |                                 |
|                   |  |                                 |
|                   |  |                                 |

## Solution Equilibria

3. Sophie Soluble and Aaron Agin are debating the solubility of lead(II) compounds. Sophie claims lead(II) carbonate is less soluble than lead(II) chloride due to its smaller  $K_{sp}$ . Aaron disagrees, arguing that lead(II) carbonate is more soluble because it dissociates into fewer ions. How can Sophie clarify that  $K_{sp}$  —not ion count—determines solubility?



4. Use tools such as a dissociation equation, an ICE table, a  $K_{sp}$  expression, and good algebra skills to calculate ion concentrations in the following solutions.
- a. 0.50 M potassium carbonate
  - b. 0.33 M aluminum bromide
  - c. a saturated solution of silver acetate at 25°C. ( $K_{sp} = 1.9 \times 10^{-3}$ )
  - d. a saturated solution of calcium hydroxide at 25°C. ( $K_{sp} = 5.0 \times 10^{-6}$ )
  - e. a saturated solution of magnesium phosphate at 25°C. ( $K_{sp} = 1.0 \times 10^{-24}$ )

### Solution Equilibria

5. Use tools such as a dissociation equation, an ICE table, a  $K_{sp}$  expression, and good algebra skills to calculate the  $K_{sp}$  for the following compounds:
- A saturated solution of calcium fluoride has the following ion concentrations at equilibrium:  
 $[Ca^{2+}] = 2.1 \times 10^{-4} \text{ M}$  and  $[F^{-}] = 4.2 \times 10^{-4} \text{ M}$
  - In a saturated solution of lead(II) hydroxide, the  $[OH^{-}]$  is measured to be  $3.0 \times 10^{-7} \text{ M}$ .
  - The molar solubility of magnesium hydroxide is  $1.12 \times 10^{-4} \text{ mol/L}$  at  $25^{\circ}\text{C}$ .
6. Calculate the solubility of the following solutions.
- Copper(I) chloride in mol/L ( $K_{sp} = 1.7 \times 10^{-7}$ )
  - Magnesium fluoride in g/L ( $K_{sp} = 5.2 \times 10^{-11}$ )
  - Calcium iodate in g/L ( $K_{sp} = 6.5 \times 10^{-6}$ )