

## Natural Frequency, Forced Vibration, and Resonance Lesson Notes

### Learning Outcomes

- How can the natural frequency of an object be controlled?
- What is resonance and when does it occur?

### Natural Frequency

- |   |   |  |  |
|---|---|--|--|
| <ul style="list-style-type: none"> <li>• <b>Natural Frequency:</b> the frequency (or set of frequencies) at which an object vibrates when struck, plucked, strummed, or otherwise disturbed.</li> <li>• The <b>timbre</b> (quality) of a sound is dependent upon the mixtures of frequencies at which the source naturally vibrates.</li> </ul> | <p><b>Dropped Pencil</b></p> <p>197 Hz</p> <p>211 Hz</p> <p>217 Hz</p> <p>289 Hz</p> <p>329 Hz</p> <p>(noisy)</p> | <p><b>Flute</b></p> <p>200 Hz</p> <p>(pure tone)</p> | <p><b>Tuba</b></p> <p>200 Hz</p> <p>400 Hz</p> <p>600 Hz</p> <p>800 Hz</p> <p>1000 Hz</p> <p>(rich sounding)</p> |
|---|---|--|--|

### Factors Affecting Natural Frequency 1

The frequency (**f**) at which an object vibrates is dependent on the speed (**v**) at which vibrations travel through it and the wavelength (**λ**) established in it.

$$f = v / \lambda$$

#### Dependence on Speed:

##### Guitar Strings

(tension and density)



##### Singing Water Goblet

(mass of water)



Source: [YouTube](#)

##### Vocal Folds

(tension and density)



Source: [Wikimedia Commons](#)

### Factors Affecting Natural Frequency 2

The dimensions (e.g., length) of an object affect its frequency since larger objects vibrate with longer wavelengths. For many vibrating objects, the **vibrational frequency** (and pitch) is inversely proportional to the object's **length**.

$$f = v / \lambda$$

## Dependence on Length:

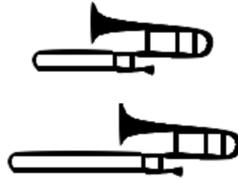
### Guitar Strings

(fingering a string)



### Trombone

(extending the slide)



### Recorder

(fingering the holes)



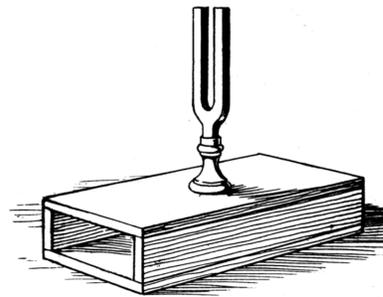
### The Straw

(cut length)



## Force Vibration

**Forced Vibration:** when one vibrating object forces another *connected* object into vibrational motion.

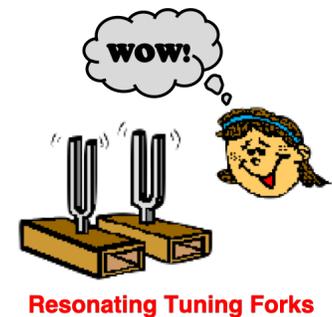


Vibrating guitar strings and tuning forks do not produce loud sounds; but when mounted on a sound box, the sound is amplified. The vibrations of the sound box force more air particles into vibration.

## Resonance

**Resonance:** when one vibrating object forces a second object to begin vibrating at the same natural frequency.

Resonance can be demonstrated with 3 sets of inverted pendula having varying length and natural frequencies.



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